How to Squash a 6-Cycle System into a Steiner Triple System

Curt Lindner

Auburn University

lindncc@auburn.edu

(joint work with Mariusz Meszka and Alex Rosa)

The spectra for Steiner triple systems and 6-cycle systems agree when $n \equiv 1$ or 9 (mod 12). Let (X, C) be a 6-cycle system of order $n \equiv 1$ or 9 (mod 12). Let T be a collection of bowties obtained by squashing each 6-cycle of C into a bowtie (i.e. identifying two 'opposite' vertices of the 6-cycle). If (X, T) is a Steiner triple system we say that the 6-cycle system (X, C) is squashed into the Steiner triple system (X, T). In this talk we construct, for every $n \equiv 1$ or 9 (mod 12) a 6-cycle system that can be squashed into a Steiner triple system.

