

Helical Compression Spring Design

QUESTION 1) A helical compression spring must give a minimum force of 500 N and a maximum force of 750 N over an adjustment range of 2 cm static deflection. The spring material is A227 cold drawn wire; the loading is static. Design the spring. ($G=79.6$ Gpa)

Solution:

$$S_{ut} = A * d^b \quad (\text{table 13-4 pp. 816})$$

$$A = 1753.3$$

$$b = -0.1822$$

$$S_{ut} = 1753.3 * d^{-0.1822}$$

$$S_{ys} = 0.6 * S_{ut} = 1051.98 * d^{-0.1822} \quad (d \text{ is in mm}), (\text{table 13-6 pp.816})$$

$$\tau_{max} = K_s \frac{8 * F * D}{\pi * d^3}$$

$$K_s = \frac{2 * C + 1}{2 * C} \Rightarrow \text{assume } C=8, \quad 4 \leq C \leq 12$$

$$K_s = \frac{17}{16} \quad \frac{D}{d} = 8 \Rightarrow D = 8 * d$$

$$\tau_{max} = \frac{17}{16} * \frac{8 * (750) * 8 * d}{\pi * d^3} = \frac{16242}{d^2}$$

$$N = \frac{S_{ys}}{\tau_{max}} = \frac{1051 * 98 * d^{-0.1822}}{\frac{16242}{d^2}} \geq 1$$

$$\Rightarrow 0.0648 * d^{2-0.1822} \geq 1$$

$$d^{1.8178} \geq 15.44$$

$$d \geq 4.5 \text{ mm}$$

$$\text{Choose A227} \Rightarrow d = 5 \text{ mm}$$

$$D = 8 * 5 = 40 \text{ mm}$$

$$N \geq 1$$

$$k = \frac{\Delta F}{y} = \frac{750 - 500}{2 * 10^{-2}} = 12500 \text{ N/m}$$

$$k = \frac{d^4 * G}{8 * D^3 * N_a} \Rightarrow N_a = \frac{d^4 * G}{8 * D^3 * k} = \frac{(5 * 10^{-3})^4 * 79.6 * 10^9 \text{ N/m}^2}{8 * (40 * 10^{-3})^3 * 12500}$$

$$N_a = 7.77 \Rightarrow N_a = 8$$

$$k = 1214.6 \text{ N/m}$$

Assume squared and ground ends,

$$N_t = 8 + 2 = 10$$

$$L_s = N_t * d = 5 * 10 = 50 \text{ mm}$$

$$y_{\text{initial}} = \frac{F_{\text{initial}}}{k} = \frac{500}{12140.6} = 0.041 \text{ m} = 41 \text{ mm}$$

$$y_{\text{clash}} = 0.15 * y = 0.15 * (20 \text{ mm}) = 3 \text{ mm}$$

$$L_f = L_s + y_{\text{clash}} + y_{\text{working}} + y_{\text{initial}} = 50 + 3 + 20 + 41 = 114 \text{ mm}$$

$$y_{\text{shut}} = L_f - L_s = 114 - 50 = 64$$

$$F_{\text{shut}} = k * y_{\text{shut}} = 1214.6 * 64 * 10^{-3} \Rightarrow F_{\text{shut}} = 777 \text{ N}$$

$$\tau_{\text{shut}} = K_s \frac{8 * F * D}{\pi * d^3} = \frac{1.06 * 8 * (777) * (40 * 10^{-3})}{\pi * (5 * 10^{-3})^3} = 671.5 \text{ MPa}$$

$$N_{s_{\text{shut}}} = \frac{S_{sy}}{\tau_{\text{shut}}} = \frac{783.88}{671.5} = 1.16 > 1$$

$$\text{Check for Buckling: } \frac{L_f}{D} = \frac{114}{40} = 2.85 < 4$$

$$\begin{aligned} \text{Inside Coil Diameter: } D_i &= D - d \\ &= 40 - 5 = 35 \text{ mm} \\ D_o &= D + d = 45 \text{ mm} \end{aligned}$$

The smallest hole:

$$\begin{aligned} \text{if } D < 13 \text{ mm} \Rightarrow \text{hole}_{\text{min}} &= D_o + 0.05 * D \\ &= 45 + 0.05 * (40) = 47 \text{ mm} \end{aligned}$$

$$\text{Clearance} = 0.1 * D$$

if $D > 13 \text{ mm}$

$$\text{Clearance} = 0.05 * D$$

The largest pin:

$$\begin{aligned} \text{pin}_{\text{max}} &= D_i - 0.05 * D \\ &= 35 - 0.05 * (40) \end{aligned}$$

$$\text{pin}_{\text{max}} = 33 \text{ mm}$$